

# Brief Article

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Homework due April 10. Have fun with these problems They are designed to get you used to the concepts.

I List all 11 graphs of order 4. (Draw them )

II. Does there exist a graph or order 5 with degree sequence

a.  $(4,4,3,2,2)$

b.  $(4,4,4,2,2)$

c.  $(2,2,2,2,2)$ . In fact, how many examples are there with this degree sequence?

Either explain why not or give an example.

III. Use the pigeonhole principal to prove that a graph of order greater than 2 always has two vertices of the same degree

In the next several problems, show how to construct it or give an example which shows you can't. In these problems, a graph of 3 or 4 vertices and a few edges will work Keep your example very simple and it will work.

Definitions of these concepts, pages bottom of 401- top of 402.

IV. Let  $x$  and  $y$  be vertices of a general graph and suppose there is a closed walk containing both  $x$  and  $y$ . Must there be a closed trail containing both  $x$  and  $y$ ?

IV. Let  $x$  and  $y$  be vertices of a general graph and suppose there is a closed trail containing them Must there be a cycle containing them?

V. Prove that if two vertices of a general graph are joined by a walk, then they are joined by a path.